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# Local Volume Tables for Young-Growth Conifers on a High Quality Site in the Northern Sierra Nevada 

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Local volume tables for ponderosa pine (Pinus ponderosa Dougl. ex Laws. var. ponderosa), sugar pine (Pinus lambertiana Dougl.), Douglas-fir (Pseudotsuga menziesii [Mirb.] Franco), Califomia white fir (Abies concolor var. lowiana [Gord.] Lemm.), and incensecedar (Libocedrus decurrens Torr.) are presented by 1 -inch diameter classes in the range of 3 to 40 inches for ponderosa pine, Douglas-fir, Califomia white fir, and incense-cedar. Sugar pine is presented to 45 inches. Trees were measured by an optical dendrometer. Tables are presented for each species in terms of cubic volume to a 0 - and 6 -inch top, and Scribner board feet to a 6 -inch top. The tables are applicable to trees growing on land of high site quality in the northem Sierra Nevada of California at low to mid elevations.

Retrieval Terms: ponderosa pine, sugar pine, Douglas-fir, Califormia white fir, incense-cedar, local volume tables

Intensive forestry requires that foresters be able to estimate tree volume accurately for such phases of timber management as timber sales, forest surveys, appraisals for land exchanges, evaluations of damage, advance planning, and growth and yield studies. The private land appraiser and even the tax assessor often find such information useful as well. Needed in particular are volume data for young trees in small-tree growth models.

To be of value, estimates of tree volume should be expressed in units of measure that relate to the products derived from the tree and that are expressed in terms familiar to the user. The board foot and cubic foot are traditional units of measure, although the cubic foot is increasing in importance as utilization of the total tree becomes more common. Consequently, future users will find volume tables more applicable if they contain both units of measure.

Future users also will find volume tables more useful if they present estimates for the species that make up the typical westside Sierra Nevada [Califomia] conifer forest. The large number of species provides raw material for a wide variety of wood products. Future managers are likely to retain the mixed-conifer forest in order to have the flexibility to capitalize on high-yielding "markets of opportunity" and to respond to the ever-changing marketplace.

From the late 1940's through the 1970's, volume estimates in Califomia were based largely on form-class volume tables derived from logged stands. ${ }^{1,2}$ But even with the
availability of such tables, those desiring a volume estimate for a specific area or range of tree size often had to construct their own local volume tables. In the mid-1970's two volume tables for softwood species in Califomia were published. ${ }^{3,4}$ Data in them vary as to source (inventory and noninventory data) and sample size, particularly with regard to trees smaller than 11 and 10 inches ( 28 and 25 cm ), respectively, in diameter at breast height (d.b.h.). In both publications, volumes for small trees are for the most part extrapolations. Needed are volume estimates, based on a full range of tree sizes, that are specific to the young-growth, mixed-conifer foreston sites of high quality in the northem Sierra Nevada of Califomia.

This note offers local volume tables that are convenient to use because the user can compare the measurements of a few trees to the values in the height-diameter figures and volume tables. If the values are close, then the tables are applicable; if not, other means of estimating volume will be needed. The local volume tables that follow contain information to a 0 -inch top (total stem), and $6-$ inch ( $15-\mathrm{cm}$ ) top for cubic feet and to a 6 inch top for Scribner board feet. The tables are based on a large sample ( 510 trees total) that reflects a special effort to sample trees in the $3-$ to 14 -inch ( $8-$ to $36-\mathrm{cm}$ ) d.b.h. range ( 89 trees). They also present volume estimates for a full range of conifer species and tree sizes typically found in a younggrowth forest in the northern Sierra Nevada at elevations from 2000 to 3500 feet ( 610 to 1068 m ).

## SITE AND GTAND

This study took place on the Challenge Erperimental Forest and surrounding area in easiem Yuba County, about 26 miles ( 42 km ) norheast of Oroville, Califomia, on land located between the south fork of the Feather Riverand the north fork of the Yuba River. Rescarch on the ExperimentalForest applies to about 1.5 million acres ( 607,035 ha) of highly productive timberland along the west slopes of the Sierra Nevada. ${ }^{5}$ These young-growth conifer and hardwood forests at low to mid-elevations form a transition zone between the chaparal and mixed hardwoods atlower elevations and the California white fir forest at higher elevations. Within this zone, and often in complex mixture, the Douglas-fir-tanoak-Pacific madrone, Pacific ponderosa pine, Pacific ponderosa pine-Douglas-fir, and Sierra Nevada mixed-conifer forest cover types are founds.

An important attribute of the Experimental Forest is is high site quality. Dominant and codominant ponderosa pines average 110 ece $(33 \mathrm{~m})$ in 50 years. ${ }^{7}$ Soils often are more then 30 feet ( 9 m ) deep as seen in road cuts, mean annual temperature is $55^{\circ} \mathrm{F}$ (13 ${ }^{\circ} \mathrm{C}$ ), and annual precipitation averages 68 inches ( 1727 mm ). Frost-free days average about 190 each year.

In stand volume, ponderosa pine (Pinus ponderosa Dougl. ex Laws. var. ponderasa) is the dominant species, followed by Douglas-fir (Pseudotsuga menziesii [Mirb.] Franco), with lesser amounts of sugar pine (Pinus lambertiana Dougl.), Califonia white fir (Abies concolor var. lowiana [Gord.] Lemm.), and incensecedar (Libocedrus decurrens Torr.). Hardwoods, principally Califomia black oak (Quercus kelloggii Newb.), tanoak (Lithocarpus densiflorus [Hook. \& Arn.] Rehd.), and Pacific madrone (Arbutus menziesii Pursh), are scattered throughout as individual trees, clumps, or groves. Average stand density in conifer and hardwood trees larger than 3.5 inches ( 8.9 cm ) d.b.h. is 248 per acre ( $613 / \mathrm{ha}$ ); basal area is $270 \mathrm{ft}^{2}$ per acre ( $62 \mathrm{~m}^{2} / \mathrm{ha}$ ). The forest is made up of a mosaic of even-age stands, depending on fire history, with the oldest dominantand codominanttrees being about 120 years old.

Sample trees were those of a forest and did not include open-grown trees in meadows or in areas with only a few remaining
seed trees. Sampledtrees did include those on ridges and in draws and in stands having a wide variety of densities and species. Trees in dense stands or growing in draws or ravines often are straight and tall with gently tapering boles, whereas trees in openings or on ridgetops often are shorter with greater taper.

## MEASUREMENTS

Because the goal was to produce an accurate local volume table representative of the Experimental Foresi and surounding area, a large, well distributed sample and anaccurate instrument were needed. Sample trees on ridges, in draws, among hardwoods, and in stands of varying density were measured with the Barr and Stroud optical dendrometer. ${ }^{8}$ Sampling followed a stratified random design. A table of diameter classes inincrements of 4 inches ( 10 cm ) was constructed for each species to ensure that a full range of trees was included in the sample.

The smallest diameter measured was 3 inches ( 8 cm ) and the largest was 40 inches ( 102 cm ), except for sugar pine, which grows rapidly on good sites, and was measured to 45 inches ( 114 cm ) d.b.h. Such diameters reflect the young-growth nature of the stands. Old-growth trees were excluded from the sample. Sampling intensity (number of trees) by species was:
ponderosa pine, 139; sugar pine, 49; Douglas-fir, 154; Califomia white fir, 80 ; and incense-cedar, 88.
For each tree, dendrometer measurements were taken at d.b.h., at one half of the branch-free bole, at the base of the live crown, at midcrown, and at the top of the tree. In addition, stump height (taken at 12 inches or 30 cm ) was measured manually. Occasionally, additional measurements of the tree bole were taken to ensure accurate volume estimates. All data were checked manually, entered on tape, and run through the STXMOD computer program which transforms tree measurements into heights, volumes, and other parameters. ${ }^{9}$ Bark thickness initially was measured directly after chopping into opposite sides of the tree. Because it conformed to values in the bark thickness tables used by the Forest Service in California, these values were adopted.
Bole volumes were computed for each species to three utilization standards: (1)
cubic foot volume to top of tree ( 0 -inch top), less a 12 -inch stump, (2) cubic foot volume to a utilized top ( 6 inches or 15 cm in diameter), less a 12 -inch stump, and (3) Scribner board-foot volume to a 6 -inch top, less a 12 -inch stump. Six inches was selected as the utilized top because this is the standard used in the majority of timber sales. Defects, including rot, crook, and sweep, were virually absent in sampled trees, and were not considered in calculating volume. The minimum log length was 10.0 feet ( 3.3 m ).

## RESULTS AND DISCUSSION

## Tree Height

The first concem that potential users of a local volume table have is the relationship of their trees to the trees in the table. Users often have a good idea of the diameterheight relationship of their trees. Consequently, graphs of height as a function of diameter (figs. 1-5) and tree height-diameter equations are presented here as a means for users of the volume tables to ascertain their applicability. Heights from the STXMOD program, plus 12 inches for stump height, were plotted against d.b.h. The relationship was tentatively expressed in several mathematical equations and examined for goodness of fit by a computerbased least-squares curve-fitting technique. The most representative equation relating total tree height ( 0 -inch top) to d.b.h. for all species was
$Y=a+b X+c X^{2}$,
in which
$Y=$ height in feet, and
$X=$ d.b.h. in inches.
Best-fit regression coefficients were:
Ponderosa pine $\quad Y=10.0333+6.3269$ $x-0.061 x^{2}$,
Sugar pine $\quad Y=-3.1144+6.8060$ $x-0.069 x^{2}$,
Douglas-fir $\quad Y=2.2668+6.8694$ $x-0.075 x^{2}$,
California white fir $Y=-5.5515+7.4811$ $x-0.082 x^{2}$, and
Incense-cedar $\quad Y=3.3860+4.8545$ $x-0.044 x^{2}$.

Correlation coefficients and standard error (in parentheses) are presented to show the goodness of fit of the regressions. Correlation coefficients, significant at the 1
percent level, were 0.85 ( 15.8 ft ) for ponderosa pine, 0.93 ( 13.1 ft ) for sugar pine, 0.93 (11.9 ft) for Douglas-fir, 0.95 ( 12.3 ft ) for Califormia white A , and 0.94 ( 11.2 ft ) for incense-cedar.

## Tree Volume

After volume as a function of d.b.h. was plotted and the general curve defined, the best mathematical expression of it was determined by a least-squares curve-fiting procedure similar to that used for tree height. Because variation in volume increased with increasing diameter, natural $\log$ d.b.h. was used to weight the regressions. The bias associated with $\log$ transformation was corrected by the equation developed by Baskerville. ${ }^{10}$ This correction was built into all the volume equations that follow. The most representative regression equation relating cubic volume to diameter was
$\operatorname{Ln} Y=a+b \operatorname{Ln} X$, in which
$Y=$ cubic foot volume $(0-$ inch
top), and
$X=$ d.b.h. in inches.

The best expressions of the relationship between cubic volume to a 0 -inch top and d.b.h. were

Ponderosa pine $\quad \mathrm{Ln}$ vol $=-4.0865$ $+2.7826 \ln$ d.b.h.,
Sugar pine Ln vol $=-3.9278$ $+2.7347 \ln$ d.b.h.,
Douglas-fir Ln vol $=-3.6083$ $+2.6516 \ln$ d.b.h.,
California white fir $\operatorname{Ln} \mathrm{vol}=-3.9320$ $+2.7749 \ln$ d.b.h., and
Incense-cedar $\quad \operatorname{Ln}$ vol $=-3.6997$ $+2.5111 \ln$ d.b.h.
Natural logarithms were used because they displayed better; data points were more spread out on graphs of the relationship. Correlation coefficients, significant at the 1 percent level, were 0.99 or better for all species. Mean squared errors, calculated from the regressions above, were 0.0224 for ponderosa pine, 0.0297 for sugar pine, 0.0346 for Douglas-fir, 0.0286 for California white fir, and 0.0250 for incense-cedar.

During development of the equation for volume to a 6 -inch top, the estimated volume equation for the 6-inch top crossed that of the 0 -inch top; in effect giving more volume to a shorter tree. Plainly, these


Figure 1-Relationship of height to diameter for ponderosa pine on the Challenge Experimental Forest, northern California.


Figure 2-Relationship of height to diameter for sugar pine on the Challenge Experimental Forest, northern California.


Figure 3-Relationship of height to diameter for Douglas-fir on the Chalienge Experimental Forest, northern California.
equations had to be developed in a slightly different manner. Close examination indicated that the difference in volume between the 0 -inch top and the 6 -inch top was roughly constant. Linear regressions of the volume difference between 0 -inch and 6inch values on d.b.h. indicated slope coefficients that did not differ significantly from zero for all species ( $p>0.05$ ). Additional calculations indicated the mean volume difference to be 1.61 cubic feet ( $0.04 \mathrm{~m}^{3}$ ) for


Figure 4-Relationship of height to diameter for California white fir on the Challenge Experimental Forest, northern California.


Figure 5- Relationship of height to diameter for incense-cedar on the Challenge Experimental Forest, northern California.
ponderosa pine, 1.51 cubic feet ( $0.04 \mathrm{~m}^{3}$ ) for sugar pine, 1.65 cubic feet ( $0.04 \mathrm{~m}^{3}$ ) for Douglas-fir, 1.58 cubic feet $\left(0.04 \mathrm{~m}^{3}\right)$ for California white fir, and 1.83 cubic feet ( $0.05 \mathrm{~m}^{3}$ ) for incense-cedar. Standard errors of these differences ranged from 0.06 to 0.09. A useful general rule of thumb for these young-growth species is that cubic volume to a 6 -inch top is about 1.7 cubic feet $\left(0.05 \mathrm{~m}^{3}\right)$ less than to a 0 -inch top.
The mathematical expression of the relationship between cubic volume to a 6 -inch top and d.b.h. is

$$
y=\exp (a+b \ln x)-c
$$

in which

$$
Y=\text { cubic volume (6-inch top) }
$$

$\exp =$ exponent of,
$\mathrm{a}=$ intercept,
$b=$ constant for volume to 0 -inch top,
$X=$ d.b.h. (inches), and
$c=a$ constant which is the mean volume difference between utilization standards.

Correlation coefficients, significant at the 1 percentlevel, were 0.98 for ponderosa pine, 0.98 for sugar pine, 0.97 for Douglas-fir, 0.98 for California white fir, and 0.98 for incense-cedar.
Sometimes, steps need to be taken to control the board-foot Scribner curve in the region of zero volume. Control near zero volume was necessary, for example, to develop the Scribner board-foot volume equations for California black oak, tanoak, and Pacific madrone in the northern Sierra Nevada. ${ }^{11}$ Specifically, it was necessary to determine the diameter at which each specics had zero board-foot volume. Although the coefficient representing the $Y$ intercept fell below zero (was negative) in the current study, this occurs only in trees that are well below the lower diameter limit for merchantable volume, and no steps to control volume near zero were attempted. The most representative Scribner board-foot volume equation for the five species proved to be

$$
\operatorname{Ln} Y=a+b \ln X
$$

in which
$Y=$ Scribner board-foot volume, and
$X=$ d.b.h. in inches.
The best expression of the relationship between Scribner board-foot volume to a 6inch top and d.b.h. for each species was

Correlation coefficients, significant at the 1 percent level, by species, and mean squared errors (in parentheses), calculated from the regression equations above, were ponderosa pine 0.98 (.0519), sugar pine 0.98 (.0874), Douglas-fir 0.96 (.0701), California white fir 0.97 (.0711), and in-cense-cedar 0.98 (.0842).

Volume tables by 1 -inch ( 2.5 cm ) diameter intervals are provided for the five conifer specics (tables 1-5). Coefficients of variation (CV) associated with predicted volume, which aid in evaluating the reliability of the volume tables, are shown as a footnote for cach table. For the 0 -inch cubic and

Table 1-Local volume table for ponderosa pine to thrae utilization standards, Challange Experimenial Forest, California

|  | Volume |  |  |
| :---: | :---: | :---: | :---: |
| D.b.h. | 0 -inch top | 6-inch iop | 6 -inch sop |
|  |  |  | Scribner |
| inches | $f^{3}$ | $f^{3}$ | board feet |
| 3 | 0.357 | - | - |
| 4 | 0.795 | - | - |
| 5 | 1.480 | - | - |
| 6 | 2.458 | - | - |
| 7 | 3.774 | - | - |
| 8 | 5.472 | 3.862 | 12.21 |
| 9 | 7.594 | 5.984 | 18.30 |
| 10 | 10.181 | 8.572 | 26.29 |
| 11 | 13.273 | 11.664 | 36.47 |
| 12 | 16.909 | 15.301 | 49.17 |
| 13 | 21.128 | 19.520 | 64.74 |
| 14 | 25.966 | 24.359 | 83.50 |
| 15 | 31.462 | 29.856 | 105.84 |
| 16 | 37.651 | 36.046 | 132.11 |
| 17 | 44.569 | 42.965 | 162.69 |
| 18 | 52.253 | 50.650 | 197.99 |
| 19 | 60.736 | 59.135 | 238.40 |
| 20 | 70.054 | 68.454 | 284.33 |
| 21 | 80.240 | 78.643 | 336.21 |
| 22 | 91.329 | 89.734 | 394.47 |
| 23 | 103.354 | 101.761 | 459.55 |
| 24 | 116.348 | 114.757 | 531.90 |
| 25 | 130.343 | 128.755 | 611.97 |
| 26 | 145.374 | 143.788 | 700.24 |
| 27 | 161.470 | 159.888 | 797.17 |
| 28 | 178.666 | 17.087 | 903.24 |
| 29 | 196.991 | 195.416 | 1018.96 |
| 30 | 216.479 | 214.907 | 1144.81 |
| 31 | 237.159 | 235.592 | 1281.30 |
| 32 | 259.064 | 257.501 | 1428.95 |
| 33 | 282.223 | 280.665 | 1588.27 |
| 34 | 306.668 | 305.115 | 1759.80 |
| 35 | 332.428 | 330.881 | 1944.05 |
| 36 | 359.534 | 357.992 | 2141.58 |
| 37 | 388.017 | 386.481 | 2352.94 |
| 38 | 417.906 | 416.376 | 2578.68 |
| 39 | 449.229 | 447.706 | 2819.35 |
| 40 | 482.019 | 480.502 | 3075.54 |
|  |  |  |  |

$\begin{array}{lcl}\begin{array}{l}\text { Coefficient of variation of } \\ \text { predicted tree volume is: }\end{array} & \\ & 21.39 & \\ 15.05 & \text { to } & 23.09 \\ & 15.10 & \end{array}$

6-inch Scribner board-foot volume tables, the coefficients were calculated by the formula

$$
C V=S Q R T \exp [M S E]-1 * 100
$$

where

$$
\begin{aligned}
M S E= & S S E /(n-2) \text { from the } \log \\
& \text { form, }
\end{aligned}
$$

and

$$
\begin{aligned}
\mathrm{SQRT} & =\text { Square root }, \\
\mathrm{MSE} & =\text { Mcan square crror, and } \\
\text { SSE } & =\text { Error sum of squares. }
\end{aligned}
$$

Table 2-Local volume table for sugar pine to three utilization standards, Challenge Experimental Forest, Calÿornia

| D.b.h. | Volume |  |  |
| :---: | :---: | :---: | :---: |
|  | 0 -inch top | 6 -inch top | 6-inch top |
| inches |  |  | Scribner board feet |
| nones | jo | $j$ | boara feet |
| 3 | 0.397 | - | - |
| 4 | 0.872 | - | - |
| 5 | 1.606 | - | - |
| 6 | 2.644 | - | - |
| 7 | 4.030 | - | - |
| 8 | 5.806 | 4.293 | 12.52 |
| 9 | 8.012 | 6.500 | 18.63 |
| 10 | 10.688 | 9.175 | 26.57 |
| 11 | 13.870 | 12.357 | 36.63 |
| 12 | 17.596 | 16.084 | 49.12 |
| 13 | 21.902 | 20.389 | 64.33 |
| 14 | 26.823 | 25.310 | 82.58 |
| 15 | 32.392 | 30.879 | 104.20 |
| 16 | 38.645 | 37.132 | 129.51 |
| 17 | 45.614 | 44.100 | 158.87 |
| 18 | 53.331 | 51.817 | 192.63 |
| 19 | 61.829 | 60.316 | 231.13 |
| 20 | 71.139 | 69.626 | 274.75 |
| 21 | 81.294 | 79.780 | 323.85 |
| 22 | 92.322 | 90.809 | 378.82 |
| 23 | 104.256 | 102.742 | 440.05 |
| 24 | 117.125 | 115.611 | 507.92 |
| 25 | 130.957 | 129.443 | 582.83 |
| 26 | 145.784 | 144.270 | 665.20 |
| 27 | 161.634 | 160.120 | 755.43 |
| 28 | 178.536 | 177.022 | 853.93 |
| 29 | 196.518 | 195.004 | 961.14 |
| 30 | 215.608 | 214.094 | 1077.48 |
| 31 | 235.835 | 234.321 | 1203.38 |
| 32 | 257.227 | 255.712 | 1339.29 |
| 33 | 279.809 | 278.294 | 1485.64 |
| 34 | 303.611 | 302.097 | 1642.90 |
| 35 | 328.658 | 327.144 | 1811.50 |
| 36 | 354.978 | 353.464 | 1991.92 |
| 37 | 382.598 | 381.083 | 2184.62 |
| 38 | 411.543 | 410.029 | 2390.07 |
| 39 | 441.840 | 440.326 | 2608.73 |
| 40 | 473.516 | 472.001 | 2841.11 |
| 41 | 506.595 | 505.080 | 3087.66 |
| 42 | 541.104 | 539.589 | 3348.89 |
| 43 | 577.067 | 575.552 | 3625.29 |
| 44 | 614.513 | 612.997 | 3917.35 |
| 45 | 653.462 | 651.948 | 4225.57 |

Coefficient of variation of
predicted tree volume is:

|  |  |  |
| :--- | :---: | :---: |
| 17.39 | 23.50 |  |
|  | 10 | 30.23 |
|  | 17.40 |  |

To account for the error introduced by the use of the correction factor in calculating the 6 -inch cubic foot volumes, the coefficient of variation was calculated by

$$
\begin{aligned}
\mathrm{CV}= & 100 * \mathrm{SQRT}\left[\mathrm{~N}^{2}(\operatorname{expN} 2-1)\right. \\
& \left.+\mathrm{N} 3^{2}\right] / \mathrm{N} 4 \text { at d.b.h. of } \mathrm{N} 0,
\end{aligned}
$$

Table 3-Local volume table for Douglas-fir to three utilization standards, Challenge Experimental Forest, California

| D.b.h. | Volume |  |  |
| :---: | :---: | :---: | :---: |
|  | 0 -inch top | 6-inch top | 6-inch top |
| inches | $f t$ | $f^{3}$ | Scribner |
| 3 | 0.499 | - | - |
| 4 | 1.070 | - | - |
| 5 | 1.933 | - | - |
| 6 | 3.135 | - | - |
| 7 | 4.718 | - | - |
| 8 | 6.723 | 5.077 | 21.02 |
| 9 | 9.187 | 7.542 | 29.99 |
| 10 | 12.149 | 10.503 | 41.22 |
| 11 | 15.642 | 13.996 | 54.95 |
| 12 | 19.701 | 18.055 | 71.45 |
| 13 | 24.359 | 22.714 | 90.97 |
| 14 | 29.648 | 28.003 | 113.77 |
| 15 | 35.599 | 33.955 | 140.10 |
| 16 | 42.244 | 40.600 | 170.22 |
| 17 | 49.611 | 47.967 | 204.39 |
| 18 | 57.730 | 56.086 | 242.86 |
| 19 | 66.629 | 64.986 | 285.90 |
| 20 | 76.336 | 74.693 | 333.76 |
| 21 | 86.879 | 85.237 | 386.70 |
| 22 | 98.284 | 96.643 | 444.98 |
| 23 | 110.579 | 108.938 | 508.85 |
| 24 | 123.790 | 122.150 | 578.58 |
| 25 | 137.941 | 136.301 | 654.43 |
| 26 | 153.059 | 151.420 | 736.65 |
| 27 | 169.169 | 167.531 | 825.50 |
| 28 | 186.294 | 184.657 | 921.25 |
| 29 | 204.460 | 202.824 | 1024.15 |
| 30 | 223.691 | 222.056 | 1134.46 |
| 31 | 244.011 | 242.377 | 1252.45 |
| 32 | 265.442 | 263.809 | 1378.37 |
| 33 | 288.008 | 286.377 | 1512.49 |
| 34 | 311.733 | 310.104 | 1655.06 |
| 35 | 336.639 | 335.010 | 1806.35 |
| 36 | 362.748 | 361.120 | 1966.61 |
| 37 | 390.082 | 388.457 | 2136.12 |
| 38 | 418.665 | 417.041 | 2315.12 |
| 39 | 448.517 | 446.895 | 2503.88 |
| 40 | 479.661 | 478.042 | 2702.67 |

Coefficient of variation of predicted tree volume is:

$$
\begin{array}{ccc} 
& 24.89 & \\
18.75 & \text { to } & 26.96 \\
& 18.83 &
\end{array}
$$

in which
$\mathrm{N} 0=$ d.b.h. (CV must be calculated for each breast height value separately),
$\mathrm{N} 1=0$-inch volume at d.b.h. N0,
$\mathrm{N} 2=$ MSE calculated for the 0 -inch regression for each species,
$\mathrm{N} 3=$ Standard error of the correction factor for volume to a 6 -inch top, and
$\mathrm{N} 4=6$-inch volume at d.b.h. N 0 .

Table 4-Local volume table for California white fir to three utilization standards, Challenge Experimental Forest, California

|  | Volume |  |  |
| :---: | :---: | :---: | :---: |
| D.b.h. | 0-inch top | 6-inch top | 6-inch top |


| D.b.h. | Volume |  |  |
| :---: | :---: | :---: | :---: |
|  | 0 -inch top | 6-inch top | 6-inch top |
| inches | $f^{3}$ | $f^{3}$ | Scribner board feet |
| 3 | 0.390 | f | - |
| 4 | 0.804 | - | - |
| 5 | 1.407 | - | - |
| 6 | 2.225 | - | - |
| 7 | 3.276 | - | - |
| 8 | 4.581 | 2.756 | 5.48 |
| 9 | 6.158 | 4.333 | 8.31 |
| 10 | 8.023 | 6.198 | 12.07 |
| 11 | 10.193 | 8.367 | 16.90 |
| 12 | 12.682 | 10.856 | 22.99 |
| 13 | 15.505 | 13.679 | 30.51 |
| 14 | 18.677 | 16.851 | 39.65 |
| 15 | 22.210 | 20.383 | 50.61 |
| 16 | 26.117 | 24.291 | 63.58 |
| 17 | 30.412 | 28.585 | 78.78 |
| 18 | 35.106 | 33.279 | 96.42 |
| 19 | 40.211 | 38.383 | 116.73 |
| 20 | 45.739 | 43.911 | 139.95 |
| 21 | 51.700 | 49.872 | 166.30 |
| 22 | 58.106 | 56.278 | 196.03 |
| 23 | 64.968 | 63.139 | 229.39 |
| 24 | 72.296 | 70.467 | 266.64 |
| 25 | 80.100 | 78.270 | 308.04 |
| 26 | 88.391 | 86.560 | 353.87 |
| 27 | 97.178 | 95.346 | 404.38 |
| 28 | 106.470 | 104.638 | 459.87 |
| 29 | 116.278 | 114.445 | 520.62 |
| 30 | 126.610 | 124.776 | 586.92 |
| 31 | 137.476 | 135.642 | 659.07 |
| 32 | 148.885 | 147.050 | 737.37 |
| 33 | 160.846 | 159.010 | 822.12 |
| 34 | 173.368 | 171.530 | 913.65 |
| 35 | 186.458 | 184.619 | 1012.26 |
| 36 | 200.125 | 198.286 | 1118.27 |
| 37 | 214.379 | 212.539 | 1232.03 |
| 38 | 229.227 | 227.386 | 1353.86 |
| 39 | 244.678 | 242.835 | 1484.09 |
| 40 | 260.738 | 258.894 | 1623.07 |

Coefficient of variation of predicted tree volume is:

|  |  |  |
| :---: | :---: | :---: |
| 15.91 | 26.68 |  |
|  | to | 29.64 |
|  | 16.02 |  |

Because the coefficient of variation for the 6 -inch cubic foot volumes is calculated at each d.b.h., it is shown as a range of values. For each species the coefficient of variation within the stated range decreases as d.b.h. increases.

The tabular values apply solely to trees having the site and stand characteristics noted earlier. The tables apply particularly to trees on sites of high quality. Deviation from high-quality sites increases the likelihood that the values will become less applicable.

## END NOTES AND REFERENCES

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